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## Channel Cooling by Turbulent Convective Mixing

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19. ABSTRACT <i>(Continue on reverse if necessary and identify by block number)</i>  Results from a series of experiments are described which show that hot, reduced-density channels in the atmosphere usually cool by a process of turbulent convective mixing. Five different types of channels were created (a) by the interaction of a pulsed CO <sub>2</sub> laser with aerosols in the atmosphere, (b) by electric discharges in the atmosphere, (c) by laser-guided, electric discharges in the atmosphere, and (d) and (e) by the absorption of CO <sub>2</sub> laser radiation in nitrogen doped with sulfur hexafluoride. For channels in which the energy deposition was almost cylindrically symmetric and axially uniform, (e), the rate of cooling, after reaching pressure equilibrium, was within an order of magnitude of thermal conduction. But for channels in which the energy deposition was asymmetric and/or non-uniform, the rate of cooling was typically one thousand times faster than thermal conduction (for channels whose radius at pressure equilibrium was ~ 1 cm). These channels were seen to be turbulent and to cool by mixing cold, surrounding air into the hot channel. Such turbulence has been explained by Picone and Boris (Ref. 5). (Continues)					
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19. ABSTRACT (Continued)

→ A simple empirical formula is deduced relating the rate of cooling (growth of channel envelope) to the radius of the channel at pressure equilibrium and to the ambient sound speed, which indicates that the effect of vorticity/turbulence saturates for variations in the energy deposition of greater than about 2 to 1.

## CONTENTS

I. INTRODUCTION .....	1
II. EXPERIMENTAL PROCEDURE .....	1
III. RESULTS AND DISCUSSION .....	5
IV. CONCLUSION .....	8
V. ACKNOWLEDGMENT .....	9
REFERENCES .....	15

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## CHANNEL COOLING BY TURBULENT CONVECTIVE MIXING

### I. INTRODUCTION

The propagation of intense particle beams, laser beams, or electric discharges through a gaseous atmosphere can result in the deposition of significant energy along the path through the atmosphere, producing a hot, reduced-density channel. The properties of the channel, in turn, affect the propagation of subsequent portions of the beam which would travel along the same path and the propagation of subsequent discharge strikes.<sup>1,2</sup> As the channel develops, these properties are determined not only by the deposition of energy that creates the channel but also by the rate of cooling. For lightning discharges in the atmosphere the rate of cooling of the hot channel also determines the chemical composition of the products.<sup>3,4</sup> In this paper we describe the results of a series of experiments which show that over a wide range of channel conditions the primary mechanism for channel cooling is turbulent convective mixing. Such turbulence has been explained by Picone and Boris<sup>5,6</sup> in terms of a residual vorticity that is caused by non-cylindrical features in the deposition of energy during the formation of the channel. For channels whose radius after reaching pressure equilibrium with the surrounding atmosphere is ~ 1 cm, cooling by turbulent convective mixing is typically one thousand times faster than thermal conduction which means that channels cool on a time scale of milliseconds rather than seconds.

### II. EXPERIMENTAL PROCEDURE

We have studied five different types of channels with very different energy deposition (from  $0.4 \text{ J/cm}^3$  to  $40 \text{ J/cm}^3$ ), with radii at pressure equilibrium varying from 0.4 cm to 2.3 cm, and with a wide range of asymmetry in the energy deposition: they are listed in Table 1. None of these channels was created by an intense particle beam but channels were created by the deposition of laser energy in gaseous atmospheres and by ohmic heating in electric discharges.

Type A). Channels of type A were produced in the laboratory atmosphere by  $\text{CO}_2$  laser-driven, aerosol-initiated, air-breakdown. The output pulse from a UV preionized, gain-switched TEA laser,<sup>7</sup> consisting of an oscillator and three

TABLE 1. Channel Cooling Studies

	Energy Deposition	Radius**	Initial Perturbation
A. CO <sub>2</sub> Laser/ Aerosols/ Atmosphere	2	2.3	very large
B. Unguided Electric Discharge	40	1.4	small
C. Laser-guided Electric Discharge	20	1.0	large
D. CO <sub>2</sub> Laser- Off-axis Modes N <sub>2</sub> + SF <sub>6</sub>	0.4	0.5	very small
E. CO <sub>2</sub> Laser- Axial Modes/ N <sub>2</sub> + SF <sub>6</sub>	0.4	0.4	negligible
	J/cm <sup>3</sup>	cm	

\*Energy Deposition is measured before expansion.

\*\*Radius is radius after expansion to pressure equilibrium [r(τ)].

amplifiers, was focused by a 3 m focal length salt (NaCl) lens. The radius of the laser beam at focus was ~ 1 cm and over an axial length of ~ 30 cm the radius remained < 1.5 cm. Breakdown occurred in this focal region during the 100 ns spike of the laser pulse and spread towards the lens during the tail of the pulse. Within the focal region breakdown occurred on many individual aerosols (Figure 1). Nearly spherical plamsas were created that grew during the tail of the laser pulse and finally coalesced to form a pseudo-cylindrical channel.<sup>8</sup> The total energy in the CO<sub>2</sub> laser pulse was ~ 1 kJ, the energy absorbed in the focal region was ~ 2 J/cm<sup>3</sup> and absorption occurred before the channel had expanded appreciably. The hot channel produced by the deposition of this laser energy expanded to reach pressure equilibrium at ~ 100  $\mu$ s when the channel radius was ~ 2.3 cm. Thereafter the channel became very turbulent and the channel envelope expanded as cold air was mixed into the channel (Figure 1).

Type B). Type B channels were produced by normal (unguided) electric discharges in the atmosphere.<sup>4</sup> A small Marx generator with an output voltage of  $\leq$  300 kV, risetime  $\leq$  100 ns, and stored energy of  $\leq$  1000 J was the source for these discharges. The discharge channel length was only ~ 20 cm, the energy deposited was ~ 40 J/cm<sup>3</sup> again calculated on the volume before any expansion had occurred, and the initial asymmetry of these channels was relatively small (Figure 2). Because all the capacitance, most of the inductance, and an appreciable fraction of the resistance (~ 50%) was within the Marx generator itself, these discharges were very reproducible electrically; period ~ 3  $\mu$ s and peak current ~ 15 kA decaying to < 1 kA in ~ 7  $\mu$ s.

Type C). Channels of Type C were produced by laser-guided, electric discharges in the atmosphere.<sup>9</sup> The path of these discharges was designated by laser-induced, aerosol-initiated air breakdown using the pulse from a Q-switched Nd:glass laser ( $\leq$  100 J in ~ 40 ns). To enhance the laser/atmosphere interaction the aerosol content of the laboratory atmosphere was increased to ~ 10<sup>-7</sup> gm/cm<sup>3</sup> by burning a small charge of black powder.<sup>10</sup> The small Marx generator, used for Type B channels, was also used as the

source for these discharges. Discharges of length up to 2 m could be produced by these techniques with a laser energy deposition of only  $\sim 15 \text{ J/m}$  within an initial channel of radius  $\sim 0.5 \text{ cm}$ . For a discharge length of 1 m, the energy deposited by the discharge channel was  $\sim 20 \text{ J/cm}^3$  ( $\sim 350 \text{ J/m}$  of channel length): the current in the discharge was a damped sinewave with peak amplitude  $\sim 10 \text{ kA}$  and period  $\sim 3 \mu\text{s}$  that decayed to  $< 1 \text{ kA}$  in  $\sim 7 \mu\text{s}$ . The use of aerosols to initiate the laser/atmosphere interaction caused these channels to have relatively large initial asymmetries (Figure 3), but not as large as those in Type A channels. These channels reached pressure equilibrium with the surrounding atmosphere  $\sim 30 \mu\text{s}$  after initiation of the Marx discharge; the channel radius was  $\sim 1 \text{ cm}$  and the channel temperature was  $\sim 5000 \text{ K}$ . Turbulent cooling became obvious for these channels after  $\sim 200 \mu\text{s}$ .

Type D and E). Both Type D channels and Type E channels were produced by the absorption of  $\text{CO}_2$  laser radiation in nitrogen doped with  $\sim 1\%$  sulfur hexafluoride.<sup>11</sup> At low laser intensities absorption of  $10.6 \mu\text{m}$  radiation excites the sulfur hexafluoride molecules but there is only slow vibrational-translational coupling to the nitrogen molecules.<sup>12</sup> However at higher laser intensities<sup>13</sup> ( $\geq 10^6 \text{ watt/cm}^2$ ) multiply excited molecules are produced and much more rapid heating of the nitrogen occurs ( $p\tau \leq 20 \mu\text{s Torr}$ ). In our experiment a 50 J pulse from the  $\text{CO}_2$  laser<sup>7</sup> was focused, using the 3 m focal length salt lens, into a long cylindrical chamber, 30 cm in diameter. The first 2.5 m of the chamber were filled with dry nitrogen, and the next 1.0 m, the interaction zone, was filled with the nitrogen/sulfur hexafluoride mixture. The fill pressure was  $\sim 900 \text{ Torr}$  and the separation of doped from undoped nitrogen was maintained by flowing the gases in at both ends of the chamber and out at a double aperture, two plates about 10 cm apart, that divided the chamber except for the 7.5 cm diameter holes at their centers. Before each laser shot the chamber was evacuated. It was filled with dry nitrogen and the flow pattern was established. Then the sulfur hexafluoride was introduced into the appropriate flow line and after the mixture had filled the interaction zone of the chamber ( $\sim 10 \text{ minutes}$ ) the experiment could proceede.

The difference between these two types of channels was in the structure of the CO<sub>2</sub> laser beam. For Type D channels the oscillator of the CO<sub>2</sub> laser used a simple "plane-plane" cavity. Thus the laser beam contained off-axis modes that came to focus at different off-axis positions. The intensity distribution in the focal region (in the interaction zone) therefore consisted of a number of "hotspots", in filaments running roughly parallel to the optic axis of the lens, with regions of lower intensity between the hotspots.

For Type E channels the oscillator of the CO<sub>2</sub> laser was reconfigured to use an off-axis confocal resonator. In such a geometry only axial modes are produced. Further, the "crescent" shaped output beam produced by the oscillator was masked with a 7.5 cm diameter aperture to select a nearly uniform, circular laser beam. In the focal region of the lens, the energy distribution from this beam was nearly azimuthally symmetric.

Channels produced by these two laser beams are shown in Figure 4. At early times ( $\sim 100 \mu\text{s}$ ) when the channels have reached pressure equilibrium but turbulence has not had time to grow, the "hot spots" in the laser beam cause the fringes in the interferogram of the Type D channels to contain sharp discontinuities. Fringes in the interferogram of the Type E channels are smooth and continuous. Type E channels did not exhibit turbulence! Apart from the mode structure in the laser beam Type D and Type E channels were very similar. The energy deposited was  $\sim 0.4 \text{ J/cm}^3$  for both channels for Type D channels the radius of the CO<sub>2</sub> laser beam was  $\sim 2.5 \text{ mm}$  and for Type E channels it was  $\sim 2.0 \text{ mm}$ . At pressure equilibrium the radii of the channels were 5 mm and 4 mm respectively.

### III. RESULTS AND DISCUSSION

For each of the five channels used in these experiments the energy was always deposited within a time,  $t_1$ , which was short compared to hydrodynamic times and within a radius  $r(1)$  which was  $\sim 1.0 \text{ cm}$ . Thus at time  $t_1$  there existed a hot channel whose density was still the ambient density but whose pressure was significantly above ambient. In the next few tens of microseconds,  $\tau \sim 30 \mu\text{s}$ , the channel expanded almost adiabatically to reach pressure equilibrium with the surrounding atmosphere. A shock wave was created during this expansion and, in some cases, some energy was lost to

radiation, but these were relatively small corrections ( $\leq 20\%$ ). If the channel had been cylindrically symmetric, as it expanded to pressure equilibrium, it would have cooled thereafter only by thermal conduction. Then the envelope of the channel would have grown as<sup>14</sup>

$$r^2(t) \sim r^2(\tau) + 4 \alpha_0 (t - \tau) ,$$

where  $\alpha_0$  is the thermal diffusivity which is  $\sim 0.2 \text{ cm}^2/\text{s}$  and  $t = \tau$  is the time at which the channel achieved pressure equilibrium. For a channel whose temperature,  $T(\tau)$  is  $\sim 3000 \text{ K}$ , the time required for the channel to cool to  $\sim 600 \text{ K}$ , i.e., for the channel radius to increase by a factor of  $\sim \sqrt{2}$ , is almost one second.

The measured growths of the five channels used in the study are shown in Figure 5. At early times the curve for each channel is linear so that unique values of a maximum anomalous diffusivity,  $\alpha$ , can be determined. This initial rate of growth increases with the initial radius of the channel,  $r(\tau)$ . At later times, channels A through D grow at increasingly slower rates (for B this flattening of the curve occurs between 20 and 30 ms).

Channels of Type E show very little growth compared to other channels, though it is still  $\sim 10$  times thermal conduction. For these channels the slope increased at later times to  $\sim 5 \text{ cm}^2/\text{s}$ .

Turbulence transports fluid properties by small scale convection. However in very simple terms, this effect may be modeled as an anomalous diffusion<sup>15</sup> in which fluid cells move a distance  $\ell$  (Prandtl eddy length) before breaking up and losing their identity. The product of this "mean free path" and the relative velocity of the fluid cell is the eddy diffusivity and becomes the effective mass diffusivity, kinematic viscosity, or thermal diffusivity. Thus we expect the thermal diffusivity to be of the form

$$\alpha \sim \ell v$$

where  $\ell$  is a characteristic length and  $v$  is a characteristic velocity. For our channels, which are to a first approximation cylindrical, the diffusion is radial. The maximum value of  $\ell$  is therefore some fraction of the radius of the channel,  $r(\cdot)$ . The maximum cell velocity is limited to some fraction of

the sound speed,  $c_s$ , of the ambient atmosphere around the channel for that is the maximum speed with which the cold fluid cells can move. With this in mind we have fitted the data for channels A through D to the relation

$$\alpha = c_s r(\tau)/k,$$

and find that

$$k = 66 \pm 6.$$

It is perhaps coincidental that the initial growth (cooling) of these four very different channels should be related in such a simple way. Certainly Picone and Paris<sup>5,6</sup> have shown that the residual vorticity, K, developed in different models for the asymmetric energy deposition is always of the form

$$K \sim u_m^2 2 \frac{r(\tau) - r(1)}{c_s} \ln (\rho_\infty / \rho_0) \cdot f$$

where  $u_m$  is a characteristic velocity of the expanding channel boundary,  $\rho_\infty$  is the ambient density,  $\rho_0$  is the minimum density in the channel, and  $f$  is a geometric form factor which is  $< 1$ . And this vorticity leads to a predicted maximum anomalous diffusivity of

$$\alpha \sim c_s \{r(\tau) - r(1)\} \ln (\rho_\infty / \rho_0) \cdot |f|/4\pi .$$

While values of the maximum anomalous diffusivity calculated from this equation<sup>4,5,6</sup> fall within a small factor ( $\lesssim 3$ ) of the measured values they do not indicate the near constant value of  $k$ . Also whereas in the experiments we see a fully developed isotropic turbulence, both theory and the numerical simulations actually deal with a residual, large scale vorticity and do not attempt to reproduce the cascade to fine scale turbulence. On the other hand the near constant value of  $k$  in the experiments suggests that the turbulence developed in the channels saturates at relatively modest levels of asymmetry in the energy deposition. However the drastic reduction in the turbulence seen in the Type E channels, and predicted from the theory in that  $f \rightarrow 0$  for these channels, is a clear indication that development of residual vorticity because of asymmetry in the energy deposition, is the mechanism that causes turbulent convective mixing.

#### IV. CONCLUSION

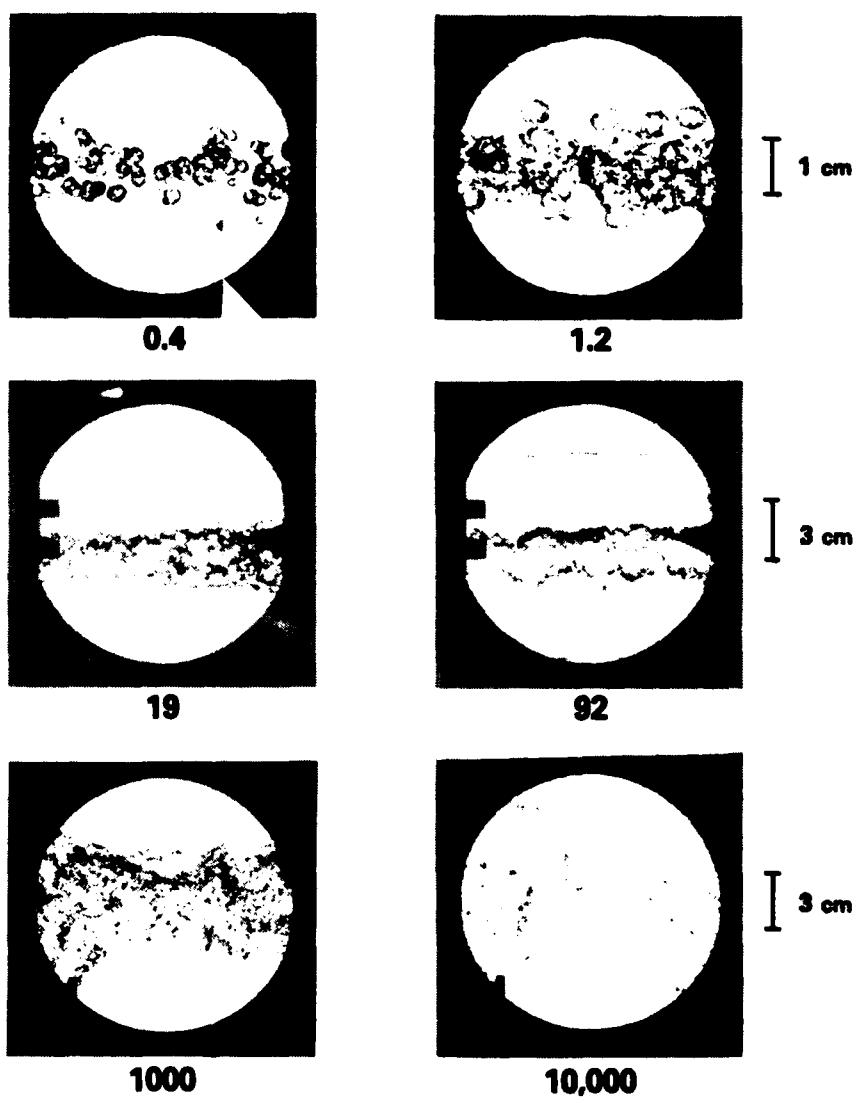
In a series of experiments we have found that hot, reduced-density channels in the atmosphere or in nitrogen at near normal temperature and pressure always cool by turbulent convective mixing provided there is more than some minimal level of asymmetry in the channel. The channels were produced by aerosol initiated, CO<sub>2</sub> laser driven air breakdown, by normal electric discharges in the atmosphere, by laser-guided, electric discharges in the atmosphere, and by the absorption of CO<sub>2</sub> laser radiation in nitrogen doped with sulfur hexafluoride. Unfortunately quantitative measurement of the azimuthal asymmetry in the channel was not possible, but it was clearly shown that elimination of the asymmetry prevented the development of turbulent convective mixing. Thus as noted by Picone and Boris<sup>4,5,6</sup> their theory for the development of vorticity and turbulent convective mixing and these experimental findings are in good agreement both in terms of identification of the mechanism for generating turbulence and in the calculation of the magnitude of the effect.

However in the experiments we have found that the anomalous diffusivity, by which the effects of turbulent convective mixing can be represented, saturates at very modest levels of asymmetry in the channel at a value dependent only on the sound speed in the ambient atmosphere and the size of the channel at pressure equilibrium. This phenomenon may well be associated with the fact that the fastest convection is always associated with the largest cells but it is not as yet predictable from the theory. It is certainly convenient that the effect of turbulent convective mixing can be represented so simply for it permits ready inclusion of this effect in channel cooling problems. For channels in the atmosphere with radius at pressure equilibrium of ~ 1 cm, the saturated anomalous diffusivity caused by turbulent convective mixing is ~ 500 cm<sup>2</sup>/s and that is ~ 2000 times larger than the effect of thermal conduction.

## V. ACKNOWLEDGMENT

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**Figure 1.** Schlieren photographs of hot channels in the atmosphere produced by aerosol-initiated, laser-driven air breakdown using a pulsed  $\text{CO}_2$  laser. Each photograph is from a different laser pulse and the time in microseconds between firing the  $\text{CO}_2$  laser and taking the photograph is shown under each photograph. The scale size for each pair of photographs is also indicated. The exposure time for each photograph is  $\sim 25$  ns. The  $\text{CO}_2$  laser enters from the left.

(TIMES IN  $\mu$ s)

250      10,000  
100      3000  
30      900  
8



**Figure 2.** Schlieren photographs of channels produced by normal (unguided) electric discharges in the atmosphere. Each photograph is from a different discharge and the time in microseconds between firing the discharge and taking the photograph is shown under each photograph. The scale size for all photographs is shown on the right. The exposure time is  $\sim 25$  ns. (This sequence was published previously in Reference 4.)

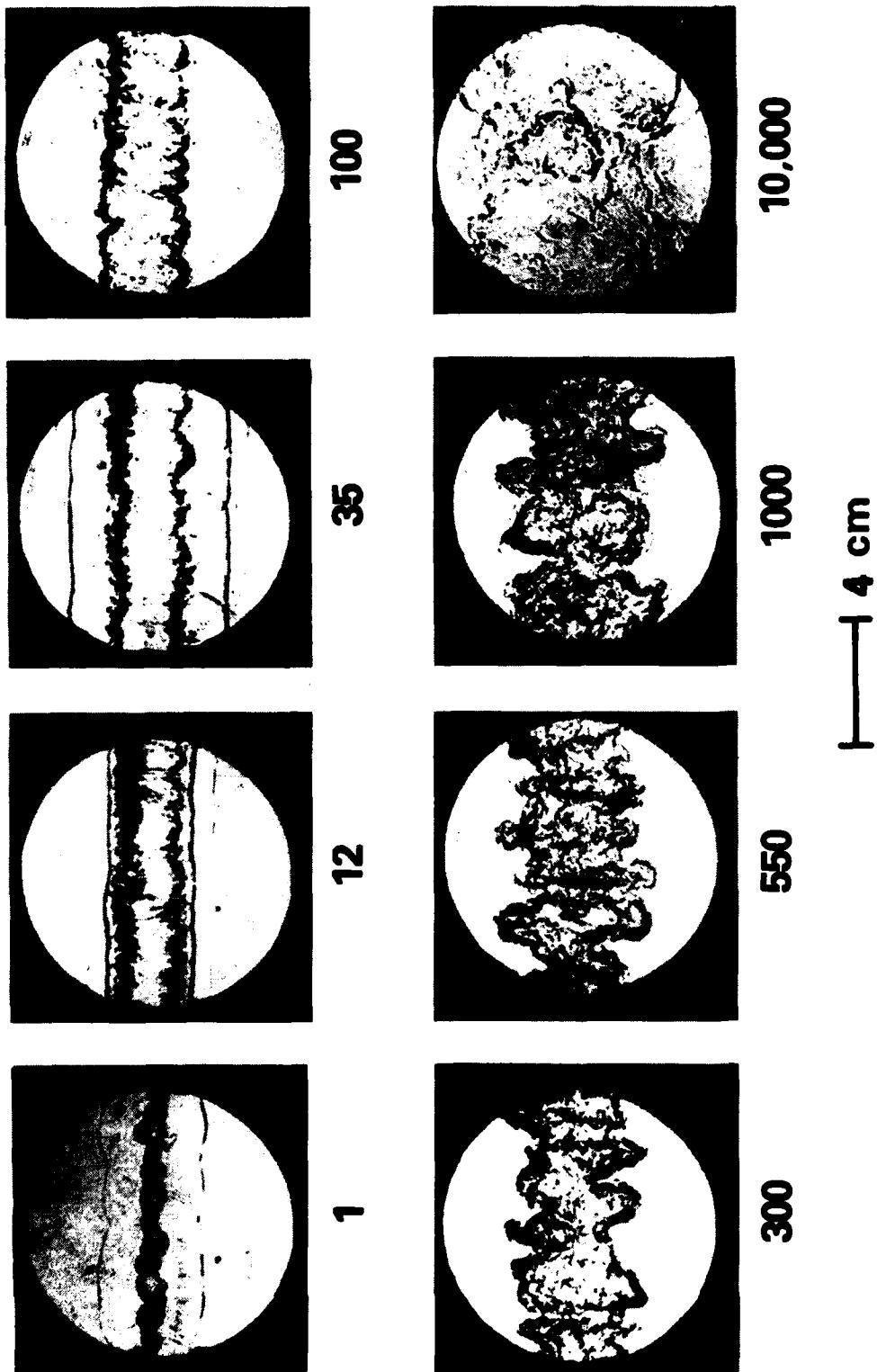


Figure 3. Schlieren photographs of channels produced by laser-guided electric discharges in the atmosphere. Each photograph is from a different discharge and shows the center section of a 1 m long discharge channel. The time in microseconds between firing the discharge and taking the photograph is shown under each photograph. The scale size for all photographs is shown and the exposure time was ~25 ns.

## CO<sub>2</sub> LASER PRODUCED CHANNELS

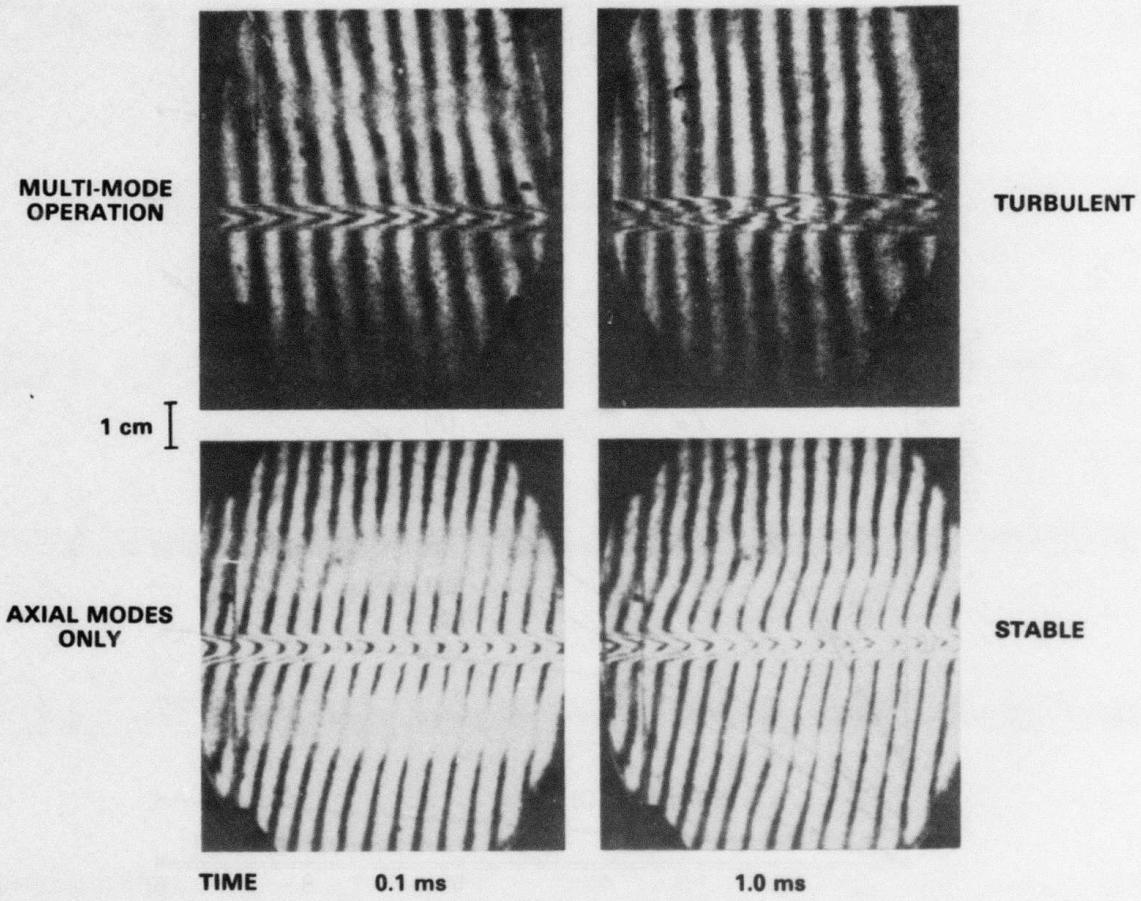


Figure 4. Interferograms of channels produced by the absorption of radiation from a pulsed CO<sub>2</sub> laser in nitrogen doped with ~ 1 % sulfur hexafluoride. The two upper photographs show the first and the tenth frames from a "movie" of a Type D channel. The two lower photographs show the same frames from a "movie" of the Type E channel. These movies were taken with a high speed framing camera using a Mach-Zehnder interferometer and a He:Ne laser. The exposure time is ~ 40  $\mu$ s and the time between frames was ~ 60  $\mu$ s (i.e., 10<sup>4</sup> frames/sec). The size scale for these photographs is indicated.

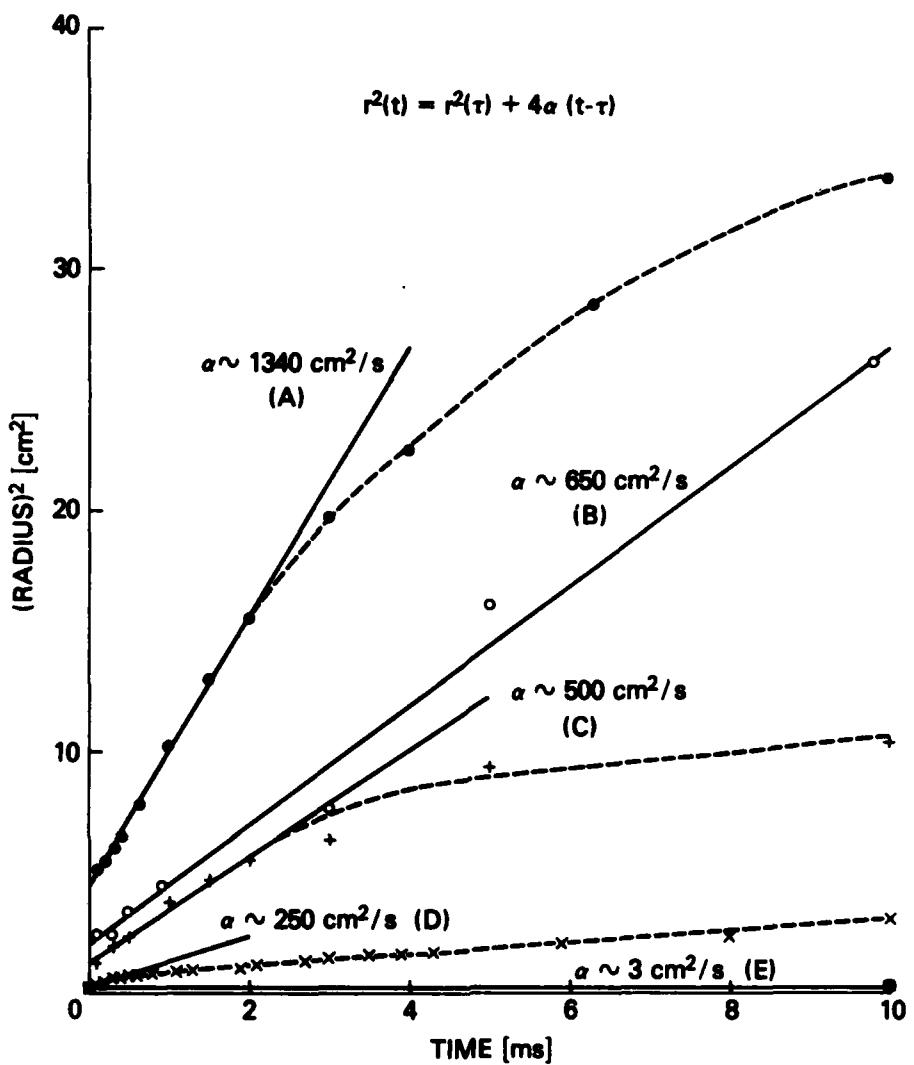


Figure 5. Variation of the measured radius of various channels with time. The channel designations A, B, C, D, and E follow from Table 1. Values of  $\alpha$  consistent with the equation

$$r^2(t) = r^2(\tau) + 4\alpha(t-\tau)$$

where  $\tau \leq 100 \mu\text{s}$  are given for the linear portion of each curve.

- Channel A
  - Channel B
  - + Channel C
  - × Channel D
  - Channel E
- } Experimental data points.

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